

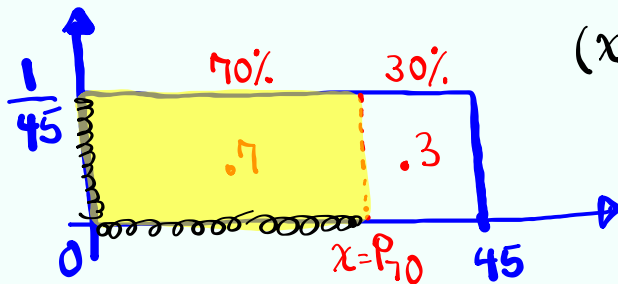
# Statistics

## Lecture 18



Feb 19-8:47 AM

Consider a uniform Prob. dist. for all values from 0 to 45. Find  $x = P_{70}$ .



$$(x - 0) \cdot \frac{1}{45} = .7$$

$$x = 45(.7)$$

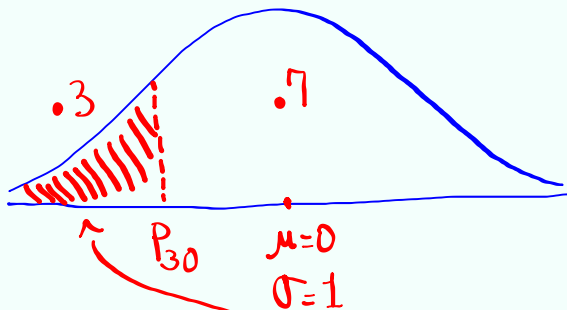
$$= \boxed{31.5} \approx 32$$

May 6-1:49 PM

find  $Z = P_{30}$ . Round to 3-dec. Places.

$$Z = \text{invNorm}(.3, 0, 1)$$

$$= \boxed{-.524}$$

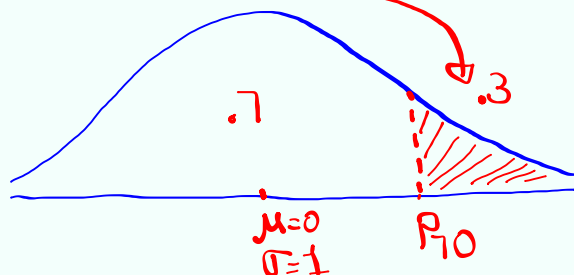


find  $Z = P_{70}$

By symmetry

$$= \boxed{.524}$$

$$Z = \text{invNorm}(.7, 0, 1)$$



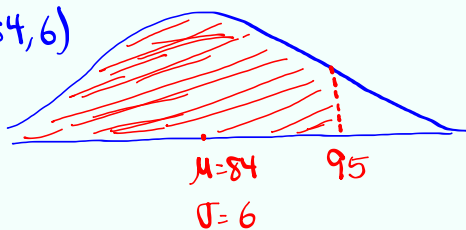
May 6-1:53 PM

Given  $N(84, 6)$  Normal Prob. dist.  
 $\mu = 84, \sigma = 6$

find  $P(x < 95)$

$$= \text{normalcdf}(-E99, 95, 84, 6)$$

$$= \boxed{.967} = 96.7\%$$

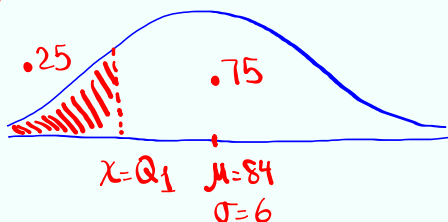


find  $x = Q_1$ , round to a whole #

$$x = \text{invNorm}(.25, 84, 6)$$

$$= 79.953$$

$$\approx \boxed{80}$$



May 6-2:00 PM

Age of Students

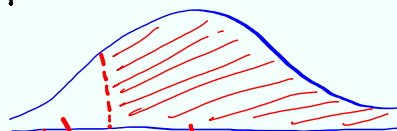
$$N(32.5, 8.2)$$

Selected groups of 4

$$P(\bar{x} > 28.5)$$

$$= \text{normalcdf}(28.5, E99, 32.5, 4.1) = .835$$

$$\text{CLT} \begin{cases} \mu_{\bar{x}} = \mu = 32.5 \\ \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{8.2}{\sqrt{4}} = 4.1 \end{cases}$$

Find  $\bar{x} = Q_3$ , round to 1-dec for groups of 4

$$\bar{x} = Q_3 = \text{invNorm}(.75, 32.5, 4.1)$$

$$= 35.265$$

$$\approx \boxed{35.3}$$



$$\text{CLT} \begin{cases} \mu_{\bar{x}} = 32.5 \\ \sigma_{\bar{x}} = 4.1 \end{cases} \quad Q_3$$

May 6-2:06 PM

Given Conf. interval  $.38 < p < .52$ 

Find

$$1) E = \frac{.52 - .38}{2} = \frac{.14}{2} = \boxed{.07}$$

$$2) \hat{p} = \frac{.52 + .38}{2} = \frac{.9}{2} = \boxed{.45}$$

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Given Conf. interval  $78 < \mu < 94$

find

$$1) E = \frac{94 - 78}{2} = \frac{16}{2} = 8$$

$$2) \bar{x} = \frac{94 + 78}{2} = \frac{172}{2} = 86$$

May 6-2:27 PM

Given  $n=150$   $x=32$  C-level = 98%.

find Conf. Interval for population Proportion

1-Prop Z Int

$$\boxed{.14 < p < .29}$$

$$E = \frac{.29 - .14}{2} = \frac{.15}{2} = \boxed{.075}$$

$$\hat{p} = \frac{.29 + .14}{2} = \frac{.43}{2} = .215 \approx \boxed{.22}$$

May 6-2:30 PM

Given :  $n = 35$     $\bar{x} = 83.5$     $\sigma = 12$

C-level : .9

Find Conf. interval for population mean

$\sigma$  Known  $\rightarrow$  Z Interval

$\sigma$  unknown  $\rightarrow$  T Interval

$$80.2 < \mu < 86.8$$

Since  $\bar{x}$  is 1-dec.  
we round to 1-dec.

$$E = \frac{86.8 - 80.2}{2} = 3.3$$

$$\bar{x} = \frac{86.8 + 80.2}{2} = 83.5$$

May 6-2:35 PM

Given :  $\bar{x} = 125$  ,  $S = 15$  ,  $n = 12$     $df = n - 1 = 11$   
NO C-level  $\rightarrow .95$

Find Conf. interval for population mean

$\sigma$  Known  $\rightarrow$  Z Interval

$\sigma$  unknown  $\rightarrow$  T Interval

$< \mu <$

$\bar{x}$  is whole #,  
round to whole #

$$E = \frac{135 - 115}{2} = 10$$

$$115 < \mu < 135$$

$$\bar{x} = \frac{135 + 115}{2} = 125$$

May 6-2:41 PM

How to find minimum sample size:

1) for proportion

$$E = z_{\alpha/2} \cdot \sqrt{\frac{\hat{p}\hat{q}}{n}} \rightarrow \text{If we solve for } n$$

$$n = \hat{p}\hat{q} \left( \frac{z_{\alpha/2}}{E} \right)^2$$

if decimal  $\rightarrow$  Always Round-up

If  $\hat{p} \neq \hat{q}$  are both unknown, use .5 for each

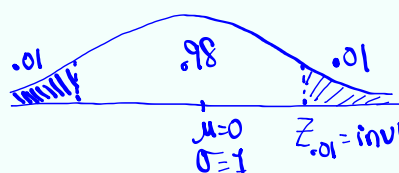
$$n = .25 \left( \frac{z_{\alpha/2}}{E} \right)^2$$

May 6-3:01 PM

find min. Sample Size needed to Construct  
98% Conf. interval for population Proportion  
with error not to exceed 5% and

1)  $\hat{p} = .4$

$\hat{q} = 1 - \hat{p} = .6$



$$n = \hat{p}\hat{q} \left( \frac{z_{\alpha/2}}{E} \right)^2$$

$$= (.4)(.6) \left( \frac{2.326}{.05} \right)^2$$

$$= 519.386$$

2)  $\hat{p} \neq \hat{q}$  are unknown

$$n \approx 520$$

$$n = .25 \left( \frac{z_{\alpha/2}}{E} \right)^2 = .25 \left( \frac{2.326}{.05} \right)^2 = 541.0276$$

$$n \approx 542$$

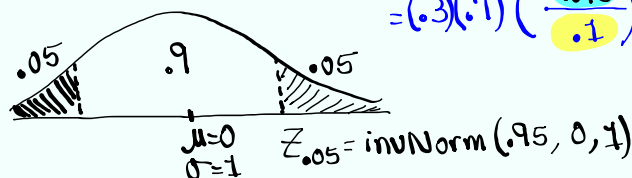
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find min. Sample Size needed to Construct  
 90% Conf. interval for pop. proportion and  
 error not to exceed 10% with

1)  $\hat{p} = .3$

$$n = \hat{p} \hat{q} \left( \frac{Z_{\alpha/2}}{E} \right)^2$$

$$= (.3)(.7) \left( \frac{1.645}{.1} \right)^2 = 56.827$$



$n \approx 57$

2) Suppose  $\hat{p} \hat{q}$  are unknown

$$n = .25 \left( \frac{Z_{\alpha/2}}{E} \right)^2 = .25 \left( \frac{1.645}{.1} \right)^2 = 67.654$$

$n = 68$

May 6-3:14 PM

min. Sample Size for population mean

$$E = Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$$

with some algebra, we solve for n.

$$n = \left( \frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2$$

If decimal,  
round-up

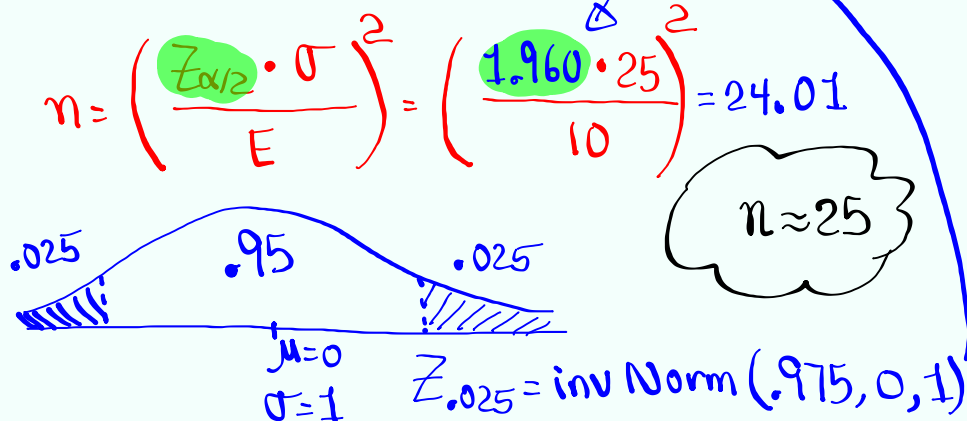
If  $\sigma$  is unknown, use S in its place.

$$n = \left( \frac{Z_{\alpha/2} \cdot S}{E} \right)^2$$

If decimal,  
round-up

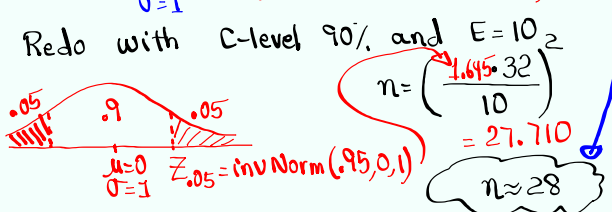
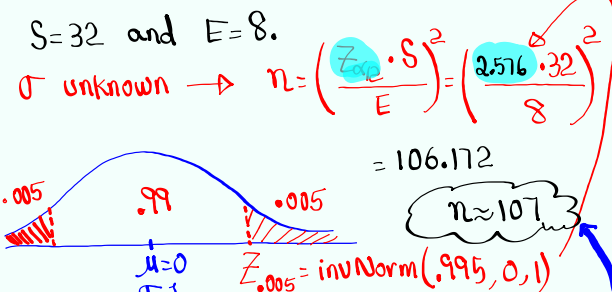
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find min. Sample Size needed to Construct 95% Conf. interval for population mean with  $\sigma = 25$  and  $E = 10$ .



May 6-3:26 PM

find min. Sample Size needed to Construct 99% Conf. interval for population mean with  $S = 32$  and  $E = 8$ .



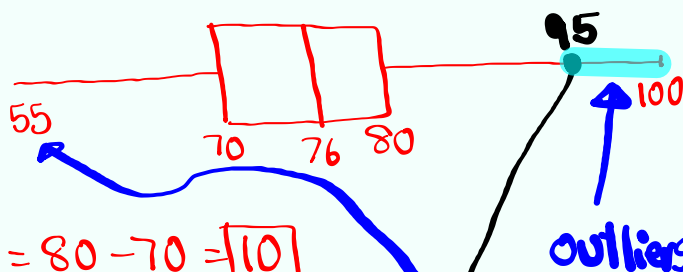
SG 21 & 22 ✓

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40 exams had the following 5-number Summary

55      70      76      80      100

1) Draw box Plot



2)  $IQR = Q_3 - Q_1 = 80 - 70 = \boxed{10}$

3) Upper & lower fences.

$$Q_3 + 1.5(IQR) = 80 + 1.5(10) = 95$$

$$Q_1 - 1.5(IQR) = 70 - 1.5(10) = 55$$

May 6-3:42 PM

40 TKTs Sold For \$10 each

one tkt drawn, winner gets a gift card worth \$100.

Find expected value per ticket sold.

Net	P(Net)
10-100	1/40
10-0	39/40

Net  $\rightarrow$  L1  
P(Net)  $\rightarrow$  L2

$$E.V. = \mu = \bar{x} = \boxed{\$7.50}$$

May 6-3:48 PM

$$P(A) = .02$$

$$1) P(\bar{A}) = 1 - P(A) = .98$$

2) odds in favor of event A.

$$P(A) : P(\bar{A}) \quad .02 : .98$$

$$\boxed{1 : 49}$$

3) odds against event A.

$$\boxed{49 : 1}$$

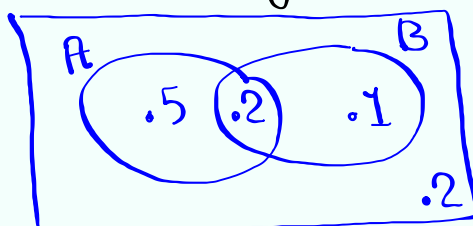
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$$P(A) = .7$$

$$P(B) = .3$$

$$P(A \text{ and } B) = .2$$

1) Venn Diagram



$$2) P(B|A) = \frac{P(A \text{ and } B)}{P(A)}$$

$$= \frac{.2}{.7} = \boxed{\frac{2}{7}}$$

$$\approx .286$$

May 6-3:58 PM